Can Decentralization Improve Social Welfare?

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3 Model Extensions



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Policy Graph Model

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A case study based on poll data

Support for legalizing marijuana



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Policy Graph Model

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- States/agents interact with neighbors in a network.
- Trade-off: Total Welfare vs border cost.
- However, former studies don't care **border cost** and are not quantified.
- We also study dynamic evolution and competition of network.

Graph Structure $\mathcal{G} = (\mathcal{P}, \mathcal{L}, \mathcal{F}, u, c)$

- Two policies: $pol_i \in \{0,1\}$, for $i \in \{1,2,\ldots,n\}$.
- Preferences $f_i = (f_{i,1}, f_{i,2})$.
- Utility:

$$u_i = egin{cases} f_{i,1} & ext{if } \textit{pol}_i = 1, \ f_{i,2} & ext{if } \textit{pol}_i = 0. \end{cases}$$

Cost:

$$c_{ij} = \begin{cases} 0 & pol_i = pol_j, \\ f_{i,2} + f_{j,1} & pol_i = 1, pol_j = 0, \\ f_{i,1} + f_{j,2} & pol_i = 0, pol_j = 1. \end{cases}$$

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Social Welfare and Optimization

Total socail welfare:

$$\tau = \sum_{i} \left(u_i - \frac{1}{2} \sum_{j}' c_{ij} \right)$$

• Goal: Maximize τ over all policy profiles, i.e.

$$pol = \arg \max_{pol \in POL} \tau.$$

Definition

$$\mu(\mathcal{G}) = \max_{\textit{pol} \notin \{\mathbf{0},\mathbf{1}\}} au - \max_{\textit{pol} \in \{\mathbf{0},\mathbf{1}\}} au$$

• Measures welfare gain from decentralized policies.

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- States 1, 2, 3 with preferences (a, 1 − a), (b, 1 − b), (c, 1 − c).
- Complete graph.
- Compute au for each of 8 policy profiles.

Preference Region Visualization

Optimal Policy Regions in (a,b,c) Space



• Clear boundary: a + b + c = 1.5.

• The powerful cost terms drives coordination behavior.

- Introduce $b_{ij} \in [0, 1]$ to control c_{ij} .
- When $b_{ij} = 0$: fully decentralized (no cross-border cost).
- When $b_{ij} = 1$: fully centralized model.

$$\tau = \sum_{i} \left(u_{i} - \frac{1}{2} \sum_{j}^{\prime} b_{ij} c_{ij} \right)$$

$$\begin{cases} \dot{f}_{i,1}(t) = \eta \cdot (1 - f_{i,1}(t)) \\ \dot{f}_{i,2}(t) = -\eta \cdot f_{i,2}(t) \end{cases} \quad \text{if } pol_i(t) = 1; \tag{1}$$

$$\begin{cases} \dot{f}_{i,1}(t) = -\eta \cdot f_{i,1}(t) \\ \dot{f}_{i,2}(t) = \eta \cdot (1 - f_{i,2}(t)) \end{cases} \quad \text{if } pol_i(t) = 2. \tag{2}$$

• Policy will influence regional preferences.

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Competition and Strategy

Example (Misreporting in Two-state Model)

Let state 1 have a preference of $f_{1,1} = 0.9$ for policy 1, and state 2 have a preference of $f_{2,1} = 0.4$. Let b_{12} denote the border influence coefficient. Here we consider party A misreporting some of its supporters in state 1, whose number is Δ .

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- Our work combines total welfare, dynamics and competition.
- Future: defining Nash Equilibrium, complexity analysis and real data modification.

Thank You!

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